TENSION-INTENSITY STRUCTURES
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The invention relates to a system of construction which utilizes the tensile properties of structural materials to the fullest advantage. It has special application to structures of vast proportions such as free-span domes capable of roof- ing a stadium or housing an entire village or city, and to mammoth air-flotable ships as well as collapsible light weight structures adapted to be transported by rocket. In general, my invention is useful wherever it is advantageous to make the largest and strongest structure per pound of structural material employed. It is applicable also to geodesic structures such as described and claimed in my prior Patent No. 2,682,235.

SUMMARY

The essence of my invention consists in the discovery of how to progressively reduce the aspect of compression in a structure so that, to a greater extent than has been found possible before, the structure will have the aspect of continuous tension throughout and the compression will be subjugated so that the compression elements become small islands in a sea of tension. This is to bring the slenderness, lightness and strength of the suspension bridge cable into the realm previously dominated by the compression column concept of building. The suspension bridge is fundamentally a tensioned structure through its use of the catenary curve of the cables between compression column towers. My invention is akin to taking some of the compression out of the “compression towers,” i.e., the columns, walls and roofs, of a building, or even taking compression out of a single column or mast through the creation of a structure having discontinuous compression (as hereinbefore defined) and continuous tension and wherein the islands of compression in the mast are progressively reduced in individual size and total mass.

As applied to a geodesic dome structure, I might describe my invention as a structure of generally spherical form comprising discontinuous compression columns arranged in an overall pattern of three-column tepee each column of each tepee being joined in “apparent” continuity to one column of one of three adjacent tepees to form what appears as a single column-like member, and the outer parts of the columns of each tepee being connected to one another only by tension elements. Tension elements also connect the outer parts of the columns to points on the columns in the region where they are joined together in apparent continuity.

As applied to structures generally, my invention consists in a structure comprising a plurality of discontinuous compression columns arranged in groups of three non-conjunctive columns connected by tension elements forming tension triangles, columns of adjacent groups being joined together in apparent continuity as above described.

According to another aspect of my invention the structure comprises an assemblage of tension and compression components arranged in a discontinuous compression system in which the compression components comprise an assemblage of compression and tension components arranged in a discontinuous compression system whereby the islands of compression in the initial discontinuous compression system are progressively diminished in size and relative mass.

Description

FIG. 1 shows the plan of a three-column tepee with connecting tension elements, called a three-strut octahedral tensile integrity unit, or “tensegrity.”

FIG. 2 shows an assemblage of the three-strut tensegrities of FIG. 1. This view is analytical, for in the actual structure struts of adjacent tensegrities are integrally joined in “apparent” compressional continuity. This actual structure is shown in FIG. 3, which otherwise corresponds to FIG. 2, and shows the discontinuous compression structural complex.

FIG. 4 is a side elevational view of the strut and tension sling component of the discontinuous compression structural complex of FIG. 3, called a “boom.”

FIG. 5 is a plan view of the boom of FIG. 4.

FIG. 6 is a sectional view taken on line 6—6 of FIG. 4.

FIG. 7 is a boom dimension schedule for a 270-boom tensegrity sphere.

FIG. 8 is a color code for assembling the booms of FIG. 7 according to one embodiment of my invention.

FIG. 9 is a further color code for assembling the booms.

FIG. 10 is a plan view of a 270-strut tensegrity obtained by following the color code of FIGS. 8 and 9.

FIG. 11 is a plan view of a 270-strut isotropic tensegrity obtained by assembling booms which are all of exactly the same design.

FIG. 12 is a diagram to explain the turbining tendencies of the thrusts of the boom ends in the tensegrity of FIG. 11, known as a “single bonded” tensegrity.

FIG. 13 is a diagram to explain the turbining tendencies of the thrusts of the boom ends in the tensegrity of FIG. 10, known as a “double bonded” tensegrity.

FIG. 14 shows a modified form of strut, or boom.

FIG. 15 is a perspective view of another modified form of boom.

FIG. 16 is a perspective view showing how the booms of FIG. 15 are interconnected in a tensegrity complex.

FIG. 17 is a plan view of a 270-strut geodesic sphere tensegrity utilizing the complex of FIG. 16.

FIG. 18 is an isometric view of a discontinuous compression column which can be used to replace the compression strut of the component shown in FIG. 4.

FIG. 19 is an enlargement of a portion of FIG. 18 showing a single strut made as a discontinuous compression column according to what may be imagined as a reduced scale version of FIG. 18. The area of FIG. 18 covered by FIG. 19 is that indicated at 19 on FIG. 18.

FIG. 20 is a top perspective view of a further modified form of boom which includes surface elements for a geodesic dome.

FIG. 21 shows an assemblage of a number of identical booms of the form shown in FIG. 20.

FIG. 22 is an enlarged cross sectional view taken as indicated at 22—22 in FIG. 21.

My tensegrity structure comprises a plurality of compression columns arranged in groups of three non-intersecting, or spaced, columns 1, crossed or overlapped to make a tripod as in an Indian tepee, FIG. 1, the columns of adjacent groups, FIG. 2, being integrally joined together, FIG. 3. FIGS. 1 and 2 are analytical, FIG. 3 showing the actual structure. FIG. 1 illustrates diagrammatically the cohering principle of the primary system as one component of my unique tensile integrity complex. This primary system, a three-strut tensile integrity unit, is termed a “tensegrity.” It will be observed from FIG. 1 that this primary system displays the six vertexes which characteristic of the octahedron, a polyhedron having three axial, six vertexes, eight faces, and twelve edges. In a spherical structural system made up of such primary octahedral tensegrities it becomes possible to omit tension wires which if present would lie along six of the twelve edges of each octahedron. The omission of such wires tends to obscure the visual appearance of the eight triangular faces of the octahedron, but does not destroy the octahedral
aspect of the primary system that is necessarily fixed and predetermined by the presence in the system of the afore
said six vertices which characterize the octahedron. Columns 1 are connected by tension elements such as wires or cables forming a tension triangle \(a-b-c\), and tension elements 3 connect the vertices \(a, b, c\) of the tension triangle to points in a line in the region where they are joined to the columns of adjacent tensegries. The dotted lines outlining the base of the tripod in FIG. 1 are theoretical and do not necessarily exist in the actual structure. If these dotted lines are considered to represent tension wires we have a complex primary octahedral tensegry system in which the compression columns 1 are separated from one another by the tension elements 2 and 3. Tension elements 2 and 3 extend throughout the structure in a continuous network, whereas columns 1, being separated from one another, do not make a continuous network and may be described as compression columns arranged discontinuously, hence “discontinuous compression columns.” Another aspect of discontinuous compression is found within a single column and will be understood from FIG. 3: the tension forces in wires 3, when combined, have components 17, acting in opposite directions. Thus the right-hand end of column 1 as viewed in FIG. 3 acts functionally as one compression column and the left-hand end acts as another compression column. Thus, if we disregard bending forces, the compression forces can approach theoretical zero at the point 18 in the column where the tension elements 3 are attached to it. This results in a separation of the compression forces in the two ends of the column. Because of this separation of the compression forces, we have again what may be described as “apparent discontinuous compression,” this time within a single column. Yet, because the two ends of the column are parts of one integral member, it appears as though there is just one compression member. Inasmuch as the foregoing analysis of the compression forces has revealed that there are really two separate compression columns within one integral member, it seems helpful to think of the columns of the adjacent groups, FIG. 2, as being joined together, FIG. 3, in “apparent” continuity, for although the continuity in a structural sense is real, in respect of functions in compression columns are said to be joined together in “apparent” continuity.” And because the tension network is continuous throughout the structure, whereas the columns are separated from one another and are supported so as to float in the network of tension wires, it has seemed appropriate to characterize the structure further as comprising compression elements which are like “islands” of compression in a “sea” of tension elements. If desired, the structure may contain tension wires as represented by the dotted lines in FIGS. 1 and 3. Such wires when used will relieve the columns of bending stresses and complete the interior tensional integrity of the octahedral system. The compression members are said to be discontinuous, because no force of compression is transmitted from one to the other as they float in a sea of tension elements.

Their positions are fixed by the octa system of the unit, although they have a turbining tendency as we shall see later. In the discontinuous compression assembly of FIG. 3, termed a complex of the primary three-strut tensegries, or a “complex tensegry,” the imaginary wires represented by the dotted lines in FIG. 1 are made unnecessary because of the arrangement of the primary tensegries in a spherical system.

In our consideration of the complex tensegry of FIG. 3, it will be observed that the terminal junctions of the several primary tensegries are all in alignment, i.e. 180° junctures, and are apparently compressionally continuous by reason of the fact that each pair of columns 1 integrally joined together, appear as a single column-like member. Because of this seeming continuity of compression from one primary tensegry to another and because the central coherence of the primary tensegries is visibly discontinuous by reason of omission of the tension elements shown by the dotted lines in FIGS. 1 and 3, the complex tensegry presents a visibly deceptive appearance to the unwary observer in which the joined tripod legs of adjacent units appear as single units and, as such, appear to be the primary “elements” of the complex tensegry, whereas, we have learned from our analysis of FIG. 1 and its relation to FIGS. 2 and 3 that our elements are the three-strut octahedrons and that the cohering principle of the simplest elements is tensegry. Notice that because the tension elements 3 connect the vertices of the tension triangle to points on the struts 1 in the region where they are joined together, a continuity of tension is created from end to end of each compression element by the tension elements 2 and 3.

In the integrated struts or columns of adjacent tensegry units we have the prefabricated component of my structure shown in FIG. 4, termed a boom, which in combination with the tension elements 2 and 3, emerges as a characteristic form which I call a "B-boom" owing to its configurational resemblance to the latter B. This boom is functionally an element of two adjacent primary tensegries by reason of the separation of the compression forces in the manner already described. In the particular embodiment of the B-boom shown in FIGS. 4–6, the compression boom takes the form of a tubular boom, as a tube of aluminum or steel, drilled to receive the wire facings of the tension slings 2, 3, and having a Round plug 16 in each end to receive a threaded fastening 5. Washers 4 at predetermined apexes of the sling triangles are adapted to receive the fastening at the ends of mating booms. If there is slack in the system it can be taken up by additional washers at the ends of the tube. The wire slings can be double as shown, or single. The mating booms are secured together by inserting one of the fastenings 5 of one boom through one of the washers 4 of the other as shown in FIGS. 1 and 4.

As an example to illustrate the best mode contemplated by me for carrying out my invention I shall describe the construction of a 270-boom tensegry geodesic sphere based upon a six-frequency subdivision of an icosahedron. This sphere will be constructed of five different boom components. The design factors for the booms are given in FIG. 7. Dimensions A–A, B–C, etc. are for the theoretical lines designated in FIG. 4. The length of all booms will be such as to subtend an angle of 25° 14' 30" of the sphere and proportional to the size of the sphere to be constructed. This length will be determined by simple trigonometric calculation in each case. Give the size of the sphere to be constructed, the factors shown in the diagrams are used as multipliers for direct calculation of the dimensions of the wire slings of the five boom components. Altitude factors are multiplied by the radius of the desired sphere, chord factors by the diameter.

The several boom components may then be colored according to the code given in FIG. 8, following which the manner of assembling them becomes merely a matter of matching colors. FIG. 10 also shows the manner of assembling the booms, in this case through identification of the several designs of boom components by a code consisting of solid and broken lines. The geodesic sphere tensegry of FIG. 10 is known as a double bonded turbo triangles complex tensegry (six frequency). “Double bonded” denotes the overlapping triangles of FIG. 10. FIG. 11 shows another embodiment of my invention also comprised of a 270-boom sphere. The turbo triangles complex tensegry. “Single bonded” denotes the non-overlapping triangles of this view. Comparing FIGS. 10 and 11 it will be noticed that in the single bonded construction the triangles are spaced apart whereas in the double bonded construction they overlap. Where the triangles are spaced apart (FIG. 11) it will be seen that a point of attachment 18 (FIG. 1) of the tension
elements 3 to the central portion of the column-like member 1 lies between the spaced triangles; and where the triangles overlap (FIG. 10) said point of attachment lies within the overlap. The significance of the difference between the single and double bonded constructions will be explained with reference to FIGS. 12 and 13 which are diagrams of the respective constructions. In both constructions the axes of the struts of each group of three are in spaced overlapping relation such that the axial thrusts of the struts at the points where they are connected by tension triangle elements will be additive to produce turbining forces tending to rotate the tension triangle. In the specific embodiments shown in FIGS. 12 and 13 this turbining tendency is counterclockwise as indicated by the arrows A. In the single bonded tensegrity, FIG. 12, the corners of adjacent tension triangles are spaced apart whereby the thrusts of adjacent discontinuous struts of adjacent tension triangles will be additive to produce turbining forces B additive to those tending to rotate the triangle as indicated at C. In the double bonded tensegrity, FIG. 13, the corners of adjacent tension triangles are overlapped whereby the thrusts of adjacent discontinuous struts of adjacent tension triangles will be additive to produce turbining forces B opposed to those tending to rotate the tension triangle.

FIG. 14 illustrates a modified form of boom having a reasonably wide girth at its center and tapered ends. Adjustable tie down sockets or dead eyes 5 provide means at one side and centrally of the boom for tensionally securing it to the ends of other booms of like construction. The boom may be made in two parts threaded into the connecting sleeve 6, furnishing means for adjusting the length of the boom. Holes 7 at the boom ends provide means for tying in to the dead eyes 5 of adjacent booms.

FIG. 15 shows another form of boom consisting of a trough-shaped member whose base 8 forms a compression column. Elevated central portions of the edges of the trough shaped member are provided with recesses 9 to receive the ends of the troughs of booms of like construction as in FIG. 16, and provide means for tensionally connecting the several booms in creating the primary and complex tensieties I have described. Here the base of the boom forms the compression column and its upper edges form the tension triangles and the tension elements connecting the vertexes of the tension triangles, positioned on the columns in the region where the columns of adjacent groups are joined together in apparent continuity, i.e. centrally of the booms. The functional equivalence of the trough boom to the strut and sling boom of FIGS. 4-6 becomes apparent when the booms are resolved as indicated by the dotted lines T in FIG. 16 and the base of the trough is regarded as an apparently continuous compression strut C forming parts of two adjacent primary tensegrity tripods. Again the tension and compression elements emerge in the characteristic form I have called a "B-boom." The booms may be traversed internally by perforated metal strips 10 welded or otherwise secured to the sides of the trough.

FIG. 17 shows a 270-strut geodetic sphere tensegrity with the tension triangles and overlying turbining triangles constructed from the trough or gutter booms of FIG. 15. The triangles, hexagons and pentagons of the tensegrity complex may be covered with any suitable plastic or metal skin such as the flanged metal pans shown at 11, 12. The triangular pans may be flat. The hexagonal and pentagonal pans may be made of fluted plastic or metal skins. A complete watershed is afforded by this construction, each gutter boom draining into the center of an adjacent boom, the booms forming a spidery pattern of eaves troughs for the surface skins.

FIG. 18 shows a discontinuous compression structure in which the double lines represent compression struts and the single lines represent tension elements. If desired, the compression columns or struts 1 of the primary and complex tensieties of FIGS. 1-3 may be replaced by discontinuous compression struts made according to FIG. 18. There results a structure comprising an assemblage of tension and compression components 1, 2 and 3 arranged in a discontinuous compression system in which the compression components 3 themselves comprise an assemblage of compression and tension components arranged in the discontinuous compression system of FIG. 18 whereby the islands of compression (1) in the initial discontinuous compression system are progressively diminished. The diminished islands of compression represented by the struts shown in FIG. 16 may in turn be replaced by discontinuous compression struts made according to what may be imagined as a reduced scale version of FIG. 18, with the result shown in FIG. 19 which is an enlargement of a portion of FIG. 18. Because of discontinuous compressions in my tensegrity complex, local tensions in the system can be tautened or released so as to permit a tensegrity sphere to be folded up for transport by plane, helicopter or rocket. Upon automatic release of tautened tensions and taking up of slack in released tensions for restoration of the original tension forces, the sphere (or dome) remembers its original shape and will resume it, thus providing a self-erecting structure.

With reference to FIGS. 20-22, I shall now describe another embodiment of my invention in which the booms also include surface elements for a geodetic dome. This boom may comprise a trough-shaped member similar to the boom shown in FIG. 15 whose base 8 forms a compression column and whose upper edges are designed to be stressed in tension. Weirs or recesses 9 are adapted to receive the ends of the troughs of booms of like construction. A pair of generally triangular sheets 13, 14 extend laterally from each edge of the trough, forming a large triangle 13 and a small triangle 14 at each side of the boom. The large triangles are at opposite ends of the boom. The same is true of the small triangles. By reason of this peculiar arrangement, an assemblage of like components to form a geodetic tensile tensegrity, FIG. 21, finds five or six large triangles 13 mating to form the surface of a pentagon or hexagon as the case may be (see the pentagons and hexagons of the tensegrity of FIG. 11), and three small triangles 14 mating to form the surface of the triangles of the tensegrity. The edges of the triangles preferably are curled into a trough-like form as at 15 to assist in forming a watershed. Also, the triangles are preferably curved into petal-like form as shown to gain an overlapping iris pattern and to accommodate the surface form of the tensile part of the boom with its sloping ends.

It will be remembered that in describing the design of a 270-boom tensegrity geodetic sphere with reference to the design factors given in FIG. 7, it was disclosed that the length of all booms will be such as to subtend an angle of 25°14'30" of the sphere. Thus the five different boom components of FIG. 7 all utilize one common length of strut, so the 270-strut tensegrity of FIG. 10 is entirely constructed from boom components utilizing this one standard-length strut. I have found that this simplification can be carried one step further by selecting the 270-strut tensieties of either FIG. 10 or FIG. 11 from one unique B-boom consisting of a standard-length strut and a standard form of tension sling. For example, I have constructed the double-bonded tensegrity of FIG. 10 entirely from one such unique B-boom design which will now be described in terms of its principles of construction. The length of the boom, as before, will be such as to subtend an angle of 25°14'30" of the desired sphere. Referring to the boom at the top of FIG. 7, the factors for designing the unique boom become:

| A-A | .187 |
| A-B | .066 |
| B-C | .187 |
| Altitude | .024 |
I claim:

1. A structure comprising a plurality of column-like members and a plurality of tension elements, the column-like members being held in axially spaced relationship to one another by the tension elements arranged as follows: each end of each column-like member is connected by tension elements both to an end portion and to a portion intermediate the ends of an adjacent column-like member.

2. A structure according to claim 1 in which that part of a column-like member which lies to one side of its central portion forms a triangular arrangement with two adjacent column-like members, and that part which lies to the other side of said central portion forms a triangular arrangement with another two adjacent column-like members, said two triangular arrangements overlapping one another.

3. A structure according to claim 1 in which that part of a column-like member which lies to one side of its central portion forms a triangular arrangement with two adjacent column-like members, and that part which lies to the other side of said central portion forms a triangular arrangement with another two adjacent column-like members, said two triangular arrangements being spaced from one another.

4. A structure according to claim 1 in which said column-like members are comprised by struts and said tension elements are comprised by cable means.

5. A structure according to claim 1 in which said column-like members are comprised by the bases of trough-shaped members and said tension elements are comprised by the edges of said trough-shaped members.

6. A structure according to claim 1 in which said column-like members comprise an assemblage of compression and tension components with compression components held in spaced relationship by the tension components.

7. In a discontinuous compression structure, a component comprising a strut and a pair of flexible tension slings each connected to an end portion and to a portion intermediate the ends of the strut, and means for connecting said slings respectively to end portions of two other components of like construction.

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